Enrollment No:	Exam Seat No:
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## **C.U.SHAH UNIVERSITY**

## **Summer Examination-2017**

**Subject Name: Engineering Mathematics-IV** 

Subject Code: 4TE04EMT1 Branch: B.Tech (Mech,Auto,EC,EE,EEE,Civil,IC)

**Semester: 4** Date: 03/05/2017 Time: 02:00 To 05:00 Marks: 70 Instructions:

- (1) Use of Programmable calculator & any other electronic instrument is prohibited.
- (2) Instructions written on main answer book are strictly to be obeyed.
- (3) Draw neat diagrams and figures (if necessary) at right places.
- (4) Assume suitable data if needed.

## Q.1 Attempt the following questions: (14)

- A) Define: Gradient of the scalar field. (1)
- **B**) If f(z) = u(x, y) + iv(x, y) is analytic then  $f'(z) = \dots$  (1)

$$(a)\frac{\partial u}{\partial x} + i\frac{\partial u}{\partial y} \qquad (b)\frac{\partial u}{\partial x} - i\frac{\partial v}{\partial x} \quad (c)\frac{\partial v}{\partial y} + i\frac{\partial v}{\partial x} \quad (d) \text{ None of these}$$

- C) True/False: The function  $f(z) = \overline{z}$  is not analytic at any point. (1)
- **D**) Write Fourier cosine transform of f(t). (1)
- **E**) State Simpson's 1/3 Rule. (1)
- **F)** True/False: In ODE number of independent variables are more than one. (1)
- G) The image of circle |z-1|=1 in the complex plane, under the mapping (1)

$$w = u + iv = \frac{1}{z}$$
 is

(a) 
$$|w-1| = 1$$
 (b)  $u^2 + v^2 = 1$  (c)  $u = \frac{1}{z}$  (d)  $v = \frac{1}{z}$ 

- **H**) The function  $u(x, y) = 2x x^2 + py^2$  is harmonic if  $p = \dots$  (1)
  - (a) 0 (b) 1 (c) 2 (d) 3
- I) Define: Solenoidal vector. (1)
- **J**) True/False: In usual notation  $\nabla = 1 E^{-1}$ . (1)
- **K**) Show that  $hD = \log(1 + \Delta)$  (2)
- **L)** If  $F = xz^3i 2x^2yz + 2yz^4k$  then find *curl F* at the point (1, -1, 1). (2)

## Attempt any four questions from Q-2 to Q-8

- Q.2 Attempt all questions (14)
- A) The following table gives the values of density of saturated water for various temperatures of saturated steam-



Temp T (C°)	100	150	200		250		300	
Density d (ng/m <sup>3</sup> )	958	917	865		799		712	
Find by interpolation, 275 °C.								(O. A)
Using Lagrange's Inte	rpolation	n ,express	$f(x) = \frac{1}{(x)^2}$	$\frac{3x^2+}{(x-1)(x-1)}$	$\frac{x+1}{(x-3)(x-3)}$	as sui	m of	(04)
partial fractions.								
				x + y +	z = 9		,	(O.4)
Apply Guass Jordan Me	thod to s	olve the e	quations	2x-3y	y + 4z = 1	13	(	(04)
				3x + 4y	y + 5z = 0	40		
Attempt all questions	;							(14)
Given that -	1.1	1.2	1.2	1 1 1	1	5	1.6	(05)
	3.403	1.2 8.781	1.3 9.129	9.45		750	10.031	
		0.701	7.127	7.73	7.	730	10.031	
Find $\frac{dy}{dx} & \frac{d^2y}{dx^2}$ at x=	1.6 .							
A river is 80 meter wid								(05)
one bank is given by the			e. Calcula	ate the a	area of c	cross se	ection of	
the river using Simpso $x = 0$ 10	$\frac{\text{n s } 3/8 \text{ J}}{20}$	30	40	50	60	70	80	
x 0 10 d 0 4	7	9	12	15	14	8	3	
Using R-K method of fourth order compute y(0.2) & y(0.4) given								
$\frac{dy}{dx} = y - \frac{2x}{y}; y(0) = 1.$			1 ,	, ,	, , ,			(04)
Attempt all questions	<b>!</b>						(	(14)
Show that $u(x, y) = 2x - x^3 + 3xy^2$ is Harmonic in some domain & find a								(05)
harmonic conjugate of		,,,, 15 11.		ii soine	doman	1 cc 11111	a a	,
Using Milne Thompso		d determ	ine the a	nalvtic	function	whose	e (	(05)
imaginary part $v(x, y)$				<i>j</i>			•	(00)
Define Mobius transfo	`		,	ohine ti	ransforn	nation	that (	(04)
maps $z_1 = 0$ , $z_2 = 1$ , $z_3 = 1$							······································	(04)
Attempt all questions		,,,	., .,	3 1.0	specific	.,.	(	(14)
Define Directional Derivative of function. Find the Directional derivative of								(05)
$\phi = xy^2 + yz^3$ at the poi								
$x\log z - y^2 = 4 \text{ at } (-1)$	,2,1).							
Define Curl of a Vector	field. Sh	ow that	A fluid mo	otion is §	given by		(	(05)

B)

C)

Q.3 A)

B)

C)

**Q.4** A)

B)

C)

Q.5 A)

 $v = (y \sin z - \sin x)i + (x \sin z + 2yz)j + (xy \cos z + y^2)k \text{ is Irrotational }.$   $\textbf{C}) \text{ Solve the initial value problem } \frac{dy}{dx} = x\sqrt{y}, y(1) = 1 \text{ \& hence find } y(1.5) \text{ by }$ (04)taking h=0.1 using Euler's method.

**(14)** Q.6 Attempt all questions

Find Fourier sine transform of  $e^{-\frac{ax}{x}}$ . (05)



<b>B</b> )	Find the Fourier cosine transform of $e^{-x^2}$ .	(05)
<b>C</b> )	Check Whether $f(z) = \cos z$ is analytic or not. If analytic, find its derivative.	(04)
Q.7 A)	Attempt all questions State Green's Theorem. Verify Green's Theorem for $\iint_{c} \left[ \left( x^{2} - 2xy \right) dx + \left( x^{2}y + 3 \right) dy \right]$ Where C is the boundary of the bounded	(14) (09)
<b>B</b> )	region by the parabola $y = x^2$ & line $y = x$ . Define: Line Integral. Find Work done if $\vec{F} = 2x^2j + 3xyk$ displace a particle in the xy-plane from $(0,0)$ to $(1,4)$ along the curve $y = 4x^2$ .	(05)
Q.8 A)	Attempt all questions State Stokes's Theorem. Verify Stokes's theorem for the vector field $\vec{F} = (x^2 - y^2)i + 2xyj$ in the rectangular region in the xy-plane bounded by	(14) (09)
<b>B</b> )	x = -a, x = a, y = 0, y = b. Define: Divergence. For which value of the component $v_3$ is $v = e^x \cos yi + e^x \sin yj + v_3k$ is Solenoidal.	(05)

